



L2: Observations of Stars

T.M. Rogers

Waves, Instabilities and Turbulence in GAJD, 8-14 July 2019 Cargese

Solar Neutrinos

RADIATIVE AND OTHER EFFECTS FROM INTERNAL WAVES
IN SOLAR AND STELLAR INTERIORS¹

WILLIAM H. PRESS

Harvard-Smithsonian Center for Astrophysics; and Department of Physics, Harvard University

Received 1980 March 31; accepted 1980 October 16

Orbits of Binary Stars

The Dynamical Tide in Close Binaries

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TIDAL FRICTION IN EARLY-TYPE STARS

PETER GOLDREICH
California Institute of Technology

AND
PHILIP D. NICHOLSON
Cornell University

Received 1988 September 8; accepted 1988 December 29

Macro-turbulence

Until very recently all observational constraints about mixing/angular momentum transport in stars came from measuring surface abundances/rotation

OBSERVATIONAL SIGNATURES OF CONVECTIVELY DRIVEN WAVES IN MASSIVE STARS

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Planetary Science Institute, Tucson, AZ 85721, USA
Received 2015 April 30; accepted 2015 May 23; published 2015 June 19

Measurements used to measure/place constraints on mixing beyond nominal convective-radiative boundary

INTERNAL GRAVITY WAVES MODULATE THE APPARENT MISALIGNMENT OF EXOPLANETS AROUND HOT STARS

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Mixing in Stars

Li DEPLETION IN F STARS

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Max-Planck-Institut für Astrophysik, Karl-Schwarzschild-Str. 4, D-85748 Garching bei München, Germany
Received 1998 June 23; accepted 1999 March 5

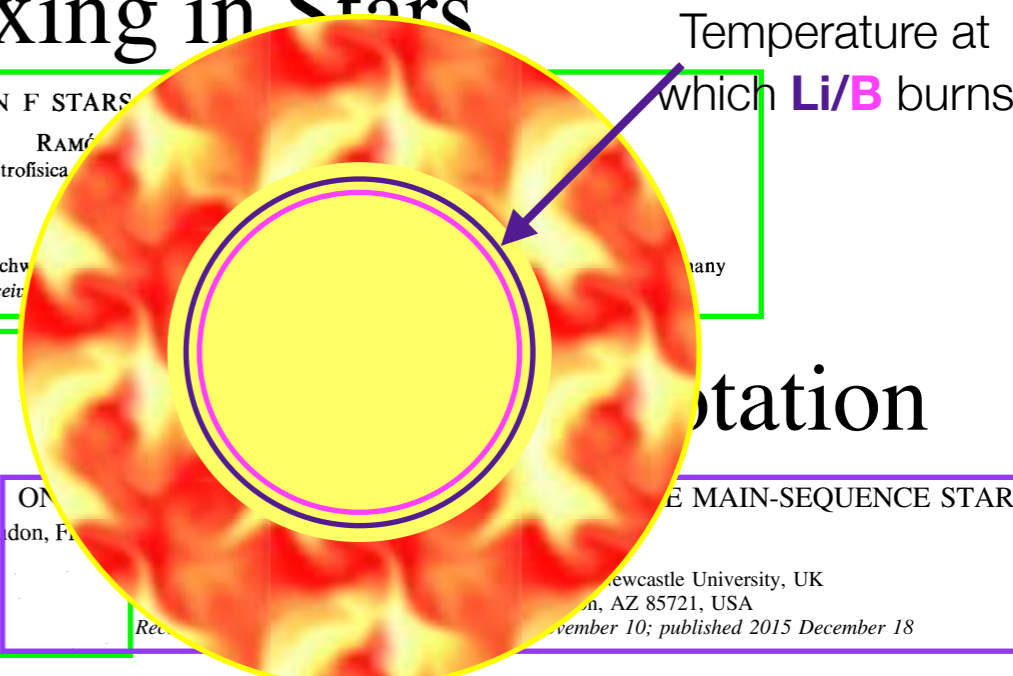
Mixing by internal waves

I. Lithium depletion in the Sun

J. Montalbán

DASGAL, Observatoire de Paris-Meudon, F-92195 Meudon, France
MESIOA::MONTALBAN (SPAN)

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Uniform Rotation of Solar Interior

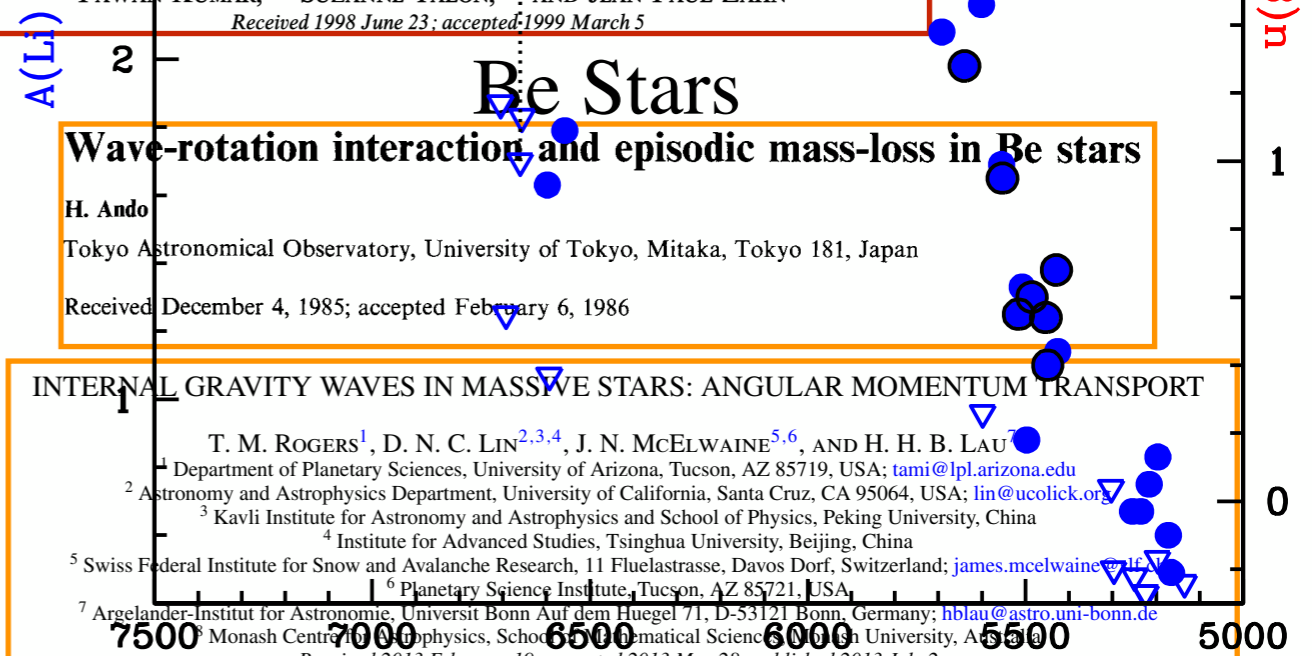
Angular momentum transport by internal waves in the solar interior

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¹ Département d'Astrophysique Stellaire et Galactique, Observatoire de Paris, Section de Meudon, 91957 Meudon, France
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ANGULAR MOMENTUM REDISTRIBUTION BY WAVES IN THE SUN

PAWAN KUMAR,^{1,2} SUZANNE TALON,³ AND JEAN-PAUL ZAHN⁵
Received 1998 June 23; accepted 1999 March 5



Wave-rotation interaction and episodic mass-loss in Be stars

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INTERNAL GRAVITY WAVES IN MASSIVE STARS: ANGULAR MOMENTUM TRANSPORT

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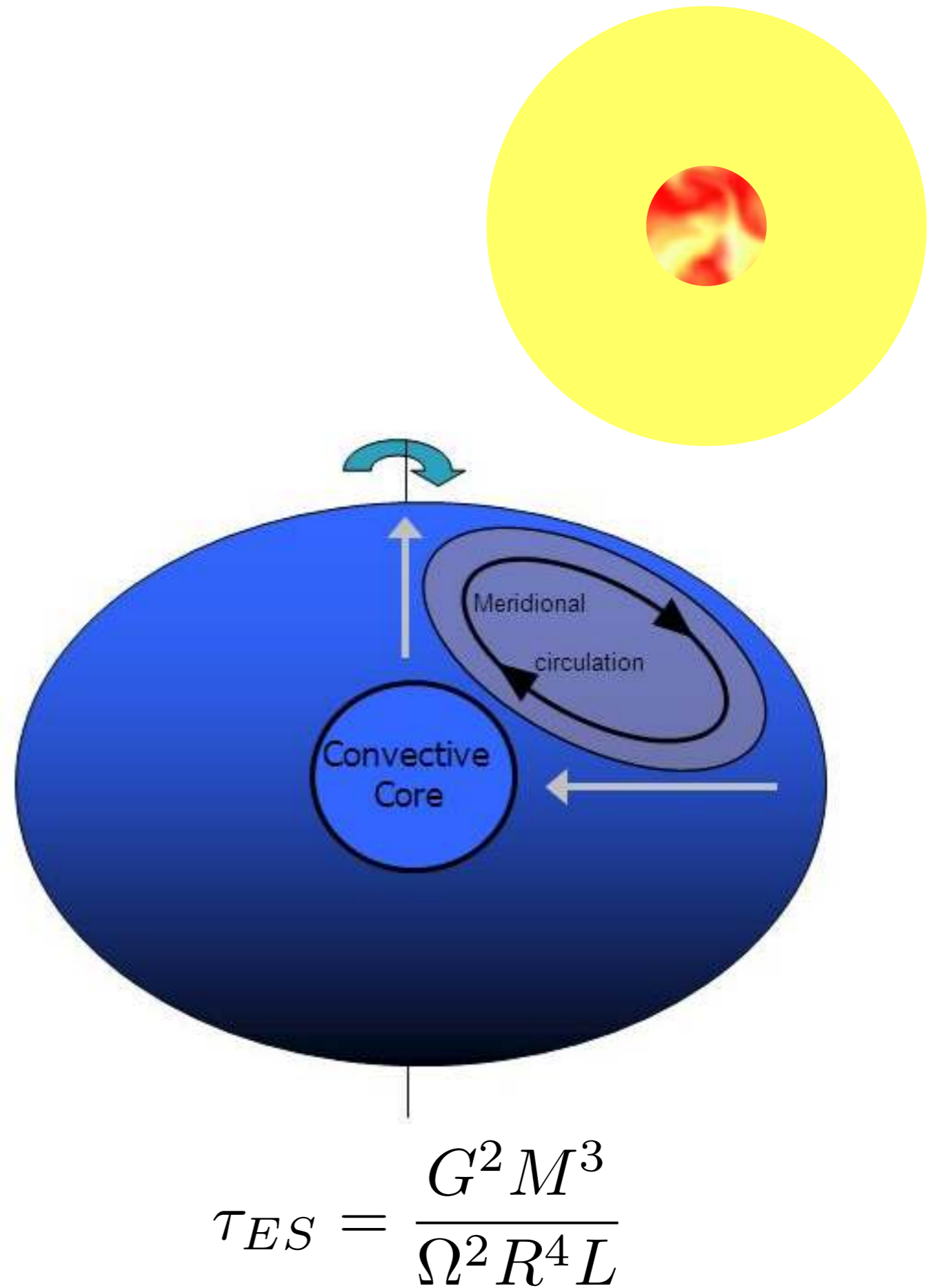
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Eddington-Sweet circulation

- Rotation causes temperature differential between pole and equator - causes meridional circulation
- Timescale inversely proportional to rotation - > fast rotation -> shorter timescales -> more efficient mixing

$$\tau_{ES\odot} \approx 10^{12} \quad \text{Not Important}$$

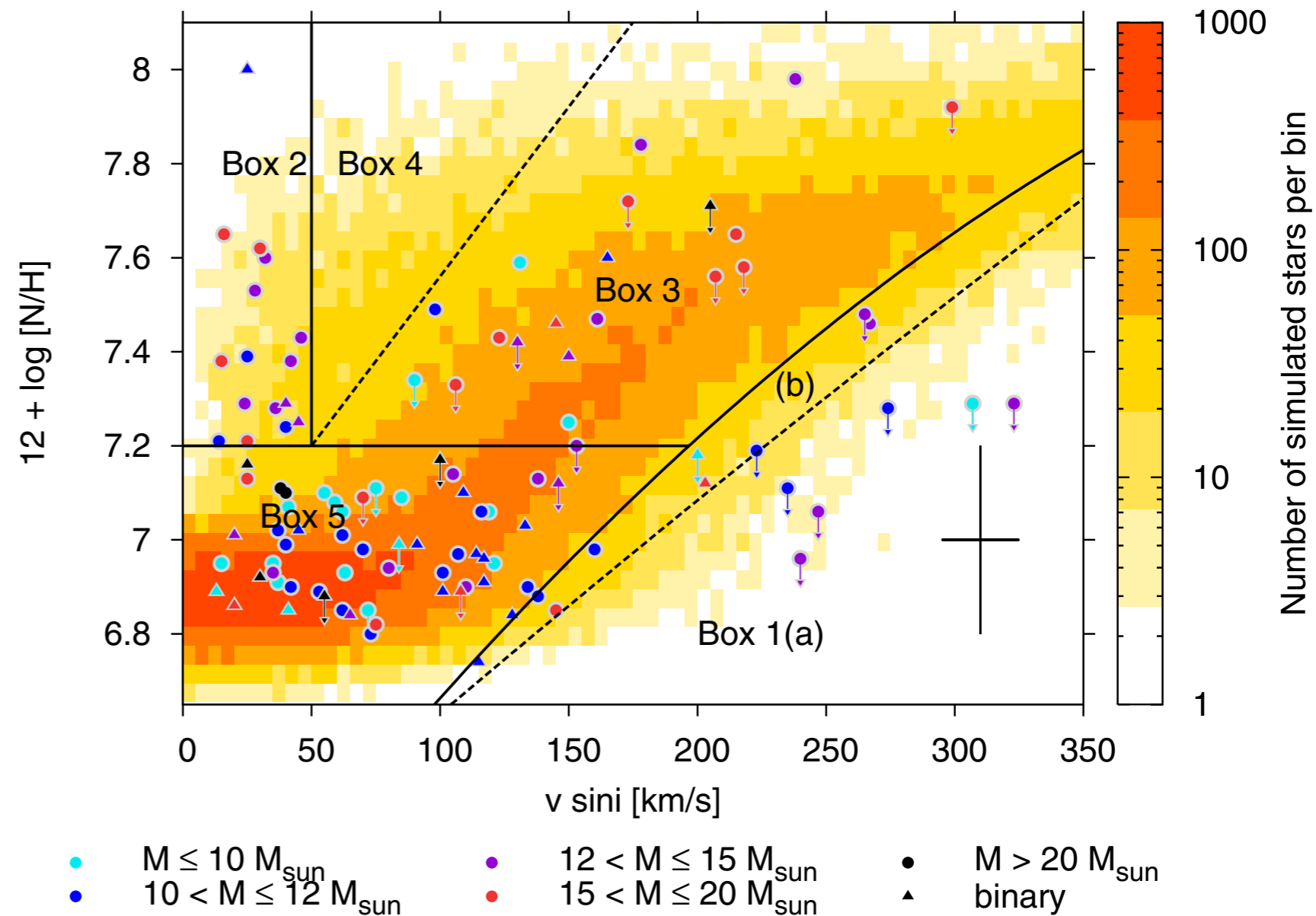
$$\tau_{ESB} \approx 10^8 \quad \text{Probably Important}$$



Chemical Mixing: Nitrogen Abundances

Brott et al. 2011

- Nitrogen is produced in the core of massive stars via burning: a surface enhancement of Ni would imply mixing through the (large) radiative envelope
- Mixing in massive stars (mostly radiative) is generally thought to be dominated by rotational mixing (Eddington-Sweet circulation)
- If this is the case one would expect strong Nitrogen enhancement at the surface of rapid rotators and no enhancement at surface of slow rotators
- This is generally seen but there are a lot of outliers : fast rotators with no enhancement + slow rotators which are enhanced



Solar Neutrinos

HeliOSEISMology

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Li DEPLETION IN F STARS BY INTERNAL GRAVITY WAVES

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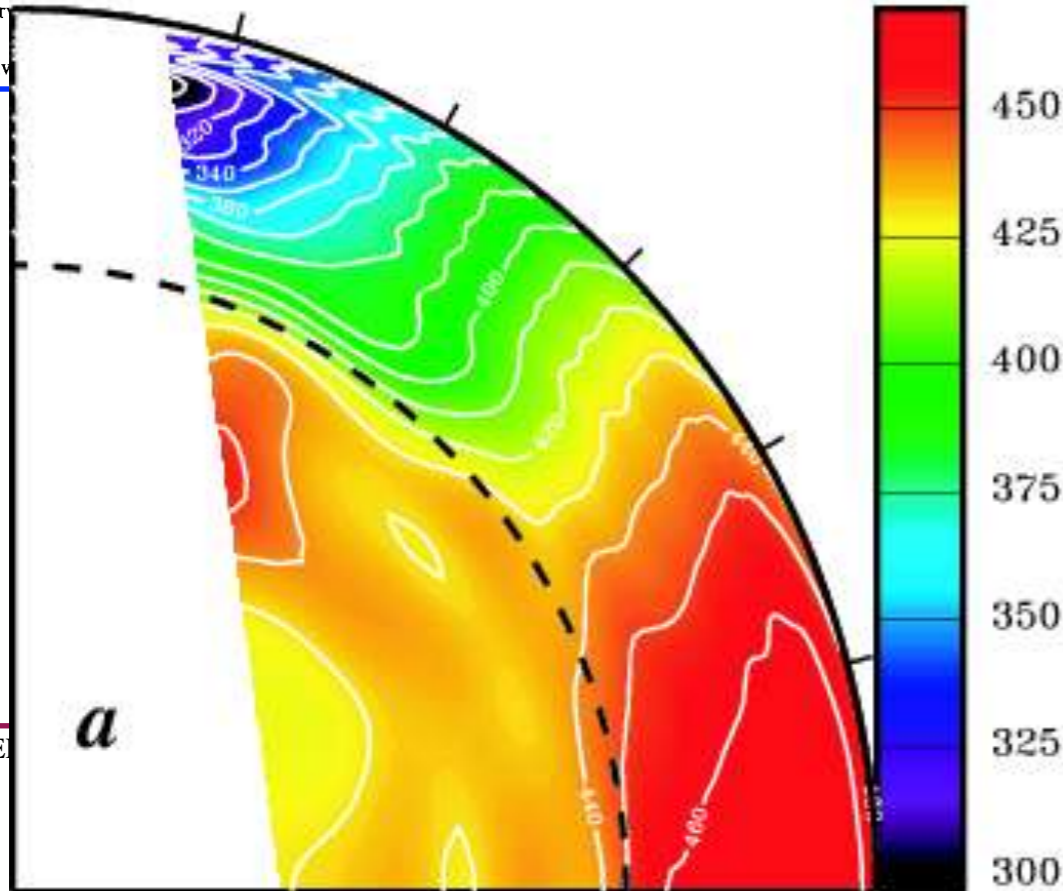
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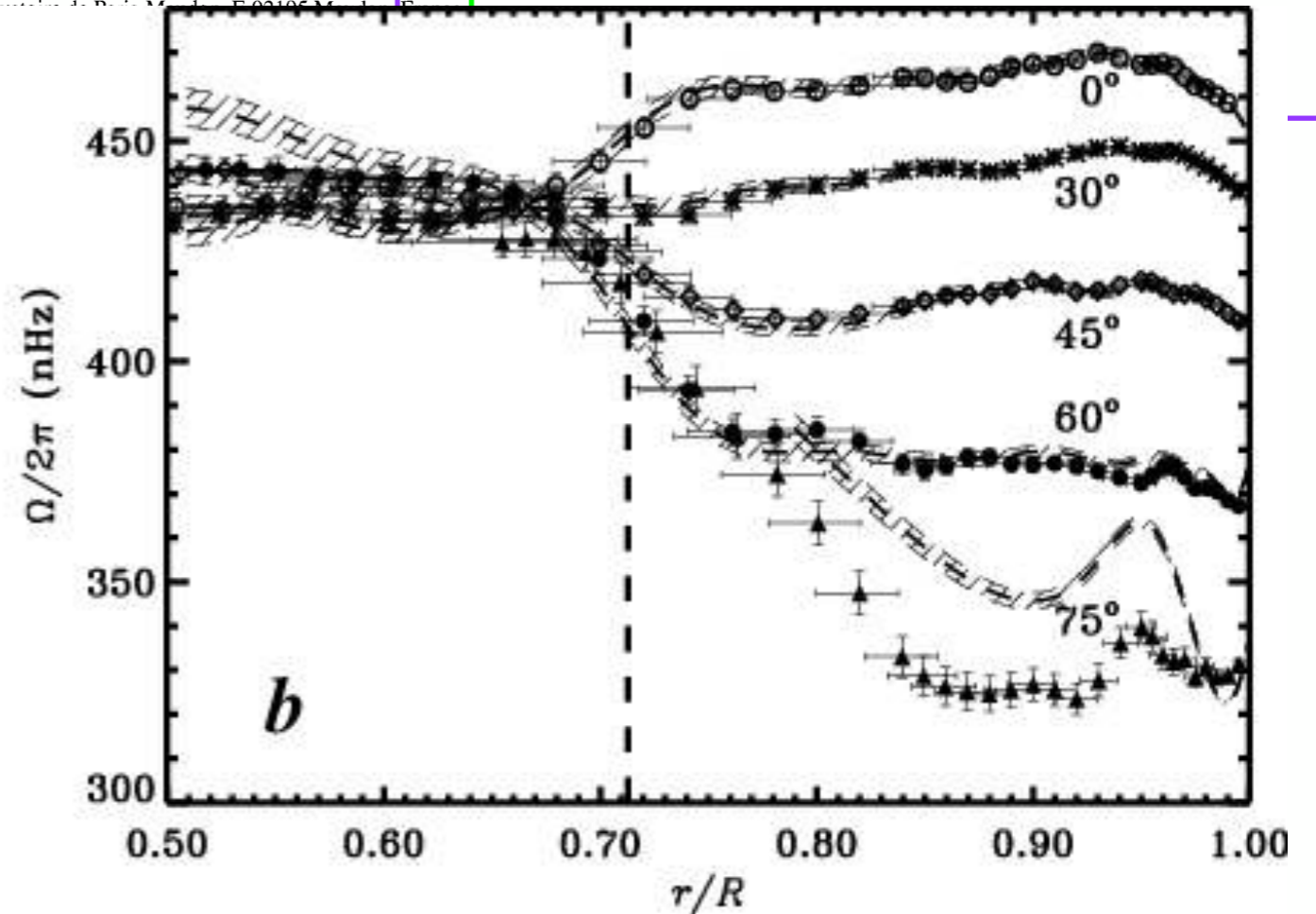
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ON THE DIFFERENTIAL ROTATION OF MASSIVE MAIN-SEQUENCE STARS



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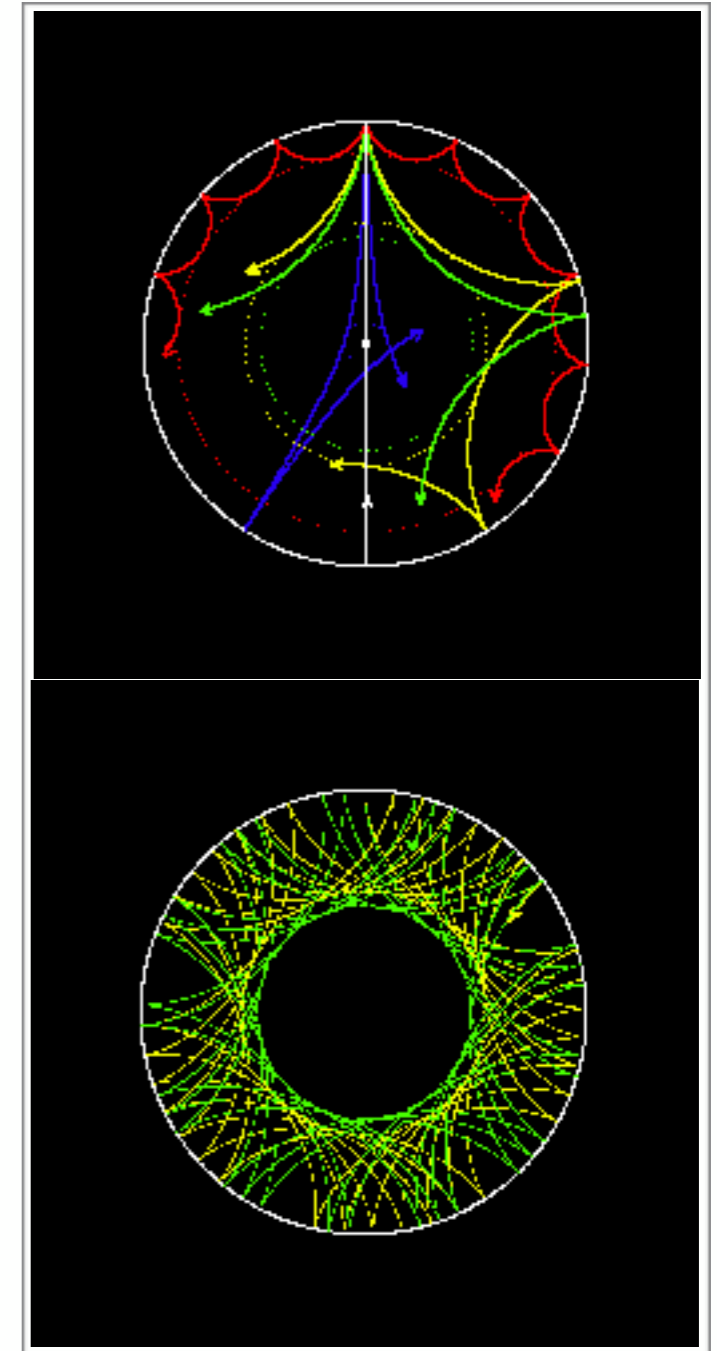
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- Radiative interior rotating uniformly
- Convective envelope rotating differentially
- Very thin layer between (tachocline)

Asteroseismology

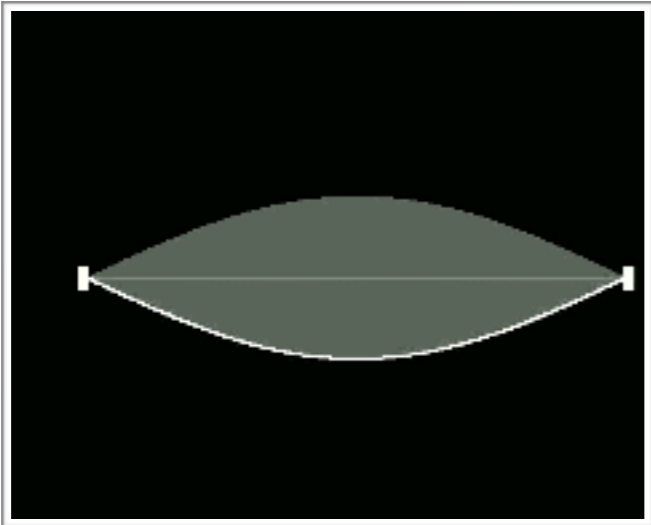
aster → star
seismos → oscillation
logos → discourse

The analysis of stellar oscillations enables the **study of the stellar interior** because different modes penetrate to different depths inside the star

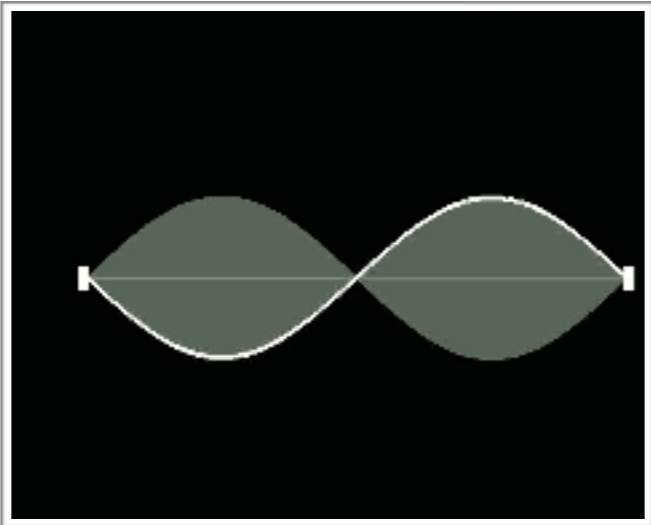


Asteroseismology 101

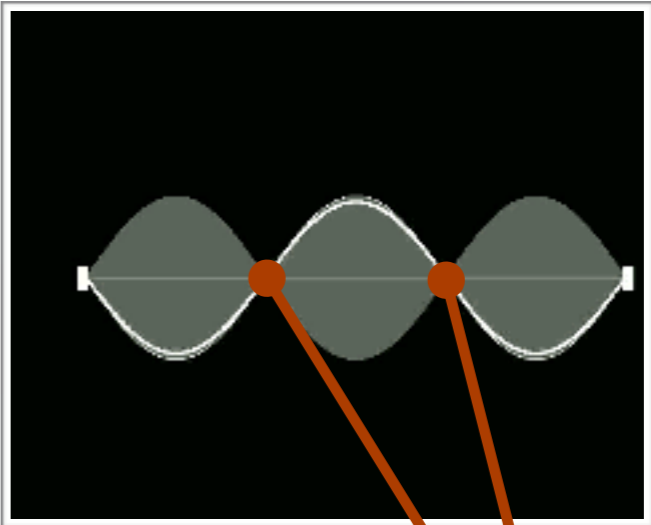
Fundamental



First overtone

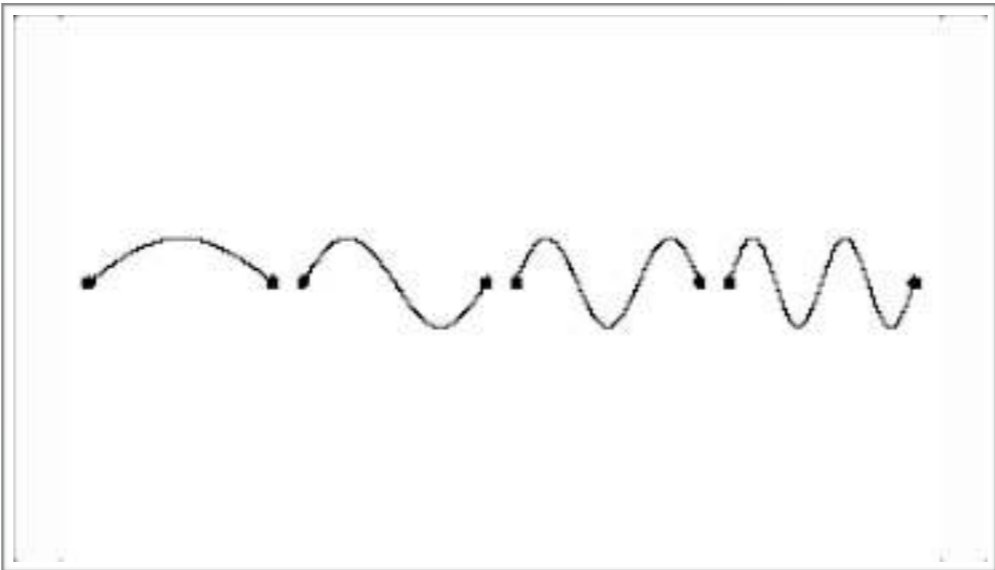


Second overtone



nodes

modes →

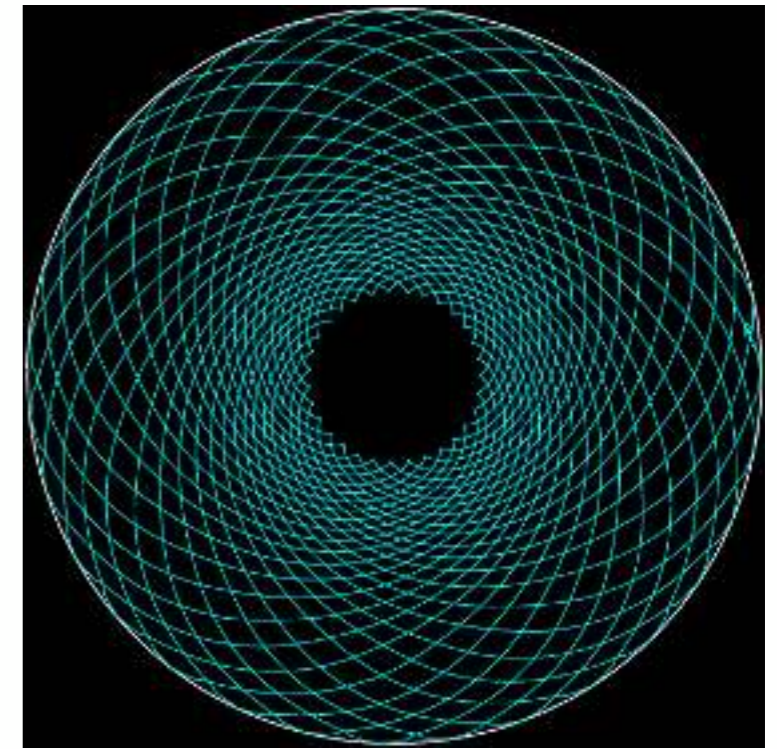


Asteroseismology

- **Oscillations = solutions of perturbed SSE in terms of periodic eigenfunctions**
- **Each oscillation mode described as spherical harmonic & frequency:**

$$\sqrt{4\pi} \Re \left\{ \left[\tilde{\xi}_r(r) Y_l^m(\theta, \phi) \mathbf{a}_r + \tilde{\xi}_h(r) \left(\frac{\partial Y_l^m}{\partial \theta} \mathbf{a}_\theta + \frac{1}{\sin \theta} \frac{\partial Y_l^m}{\partial \phi} \mathbf{a}_\phi \right) \right] \exp(-i\omega t) \right\}$$

- **Dominance of restoring force?**
 1. **pressure (acoustic waves)**
 2. **buoyancy (gravity waves)**
 3. **Coriolis (inertial waves)**
 4. **Lorentz (Alfvén waves)**
 5. **tidal (tidal waves)**



Gravity waves propagating in radiative zone of a massive star, from surface to core

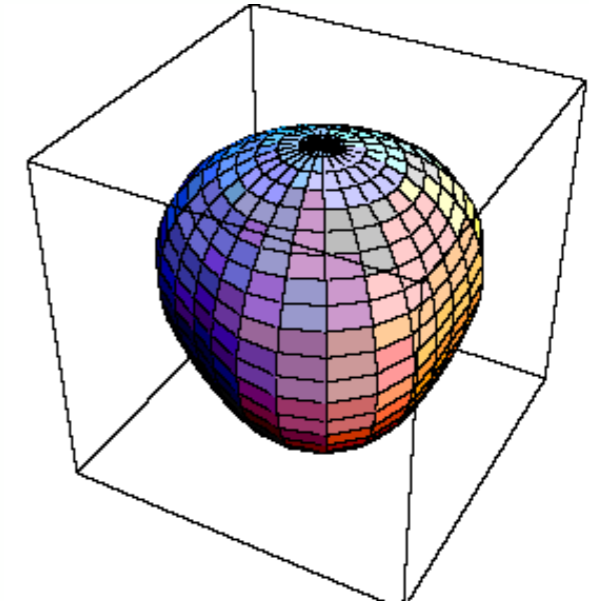
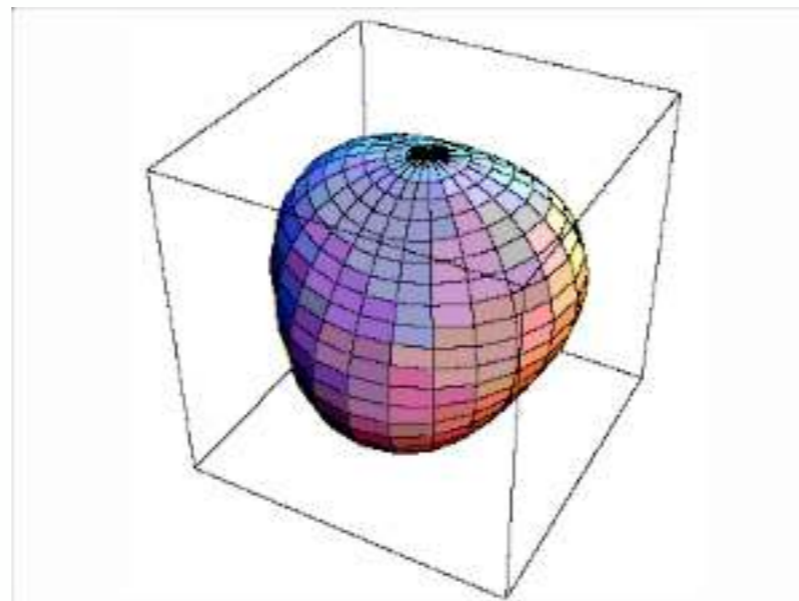
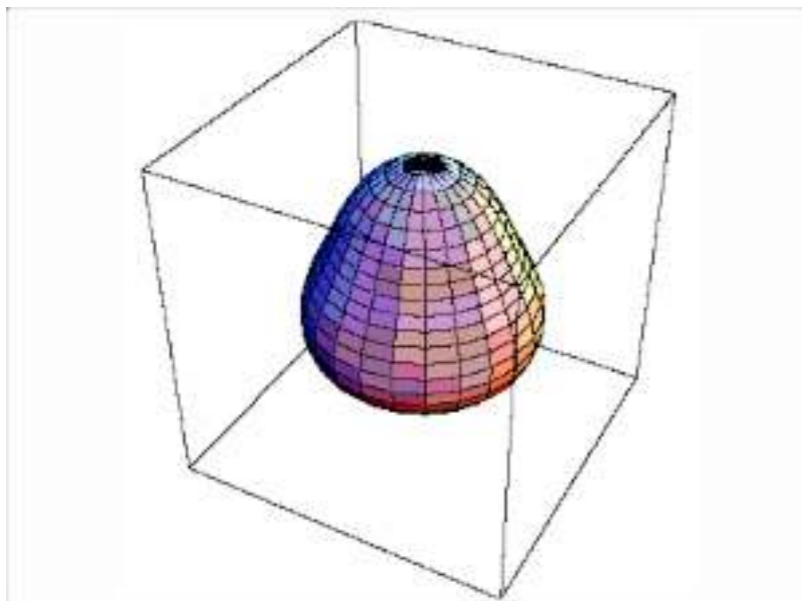
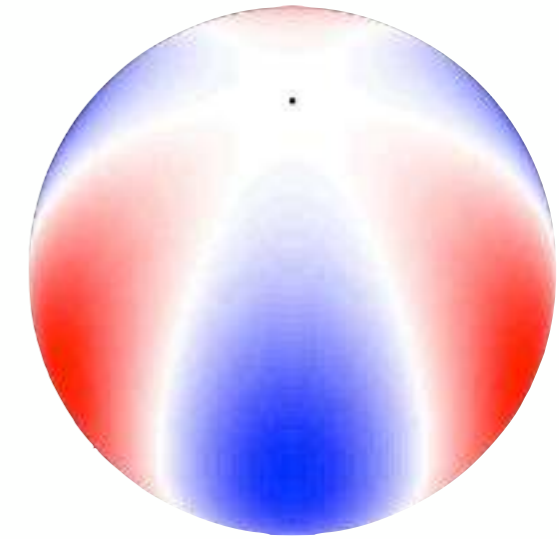
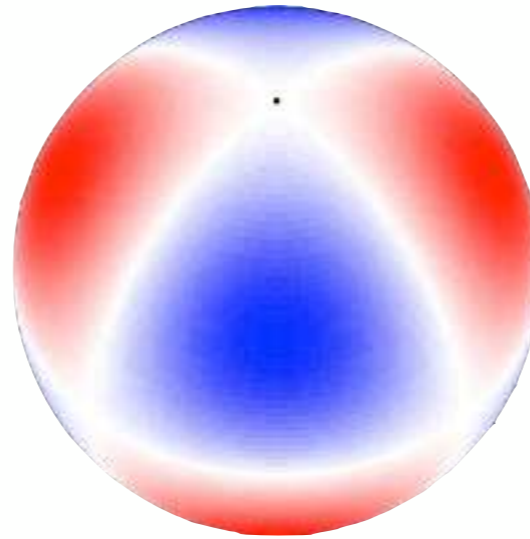
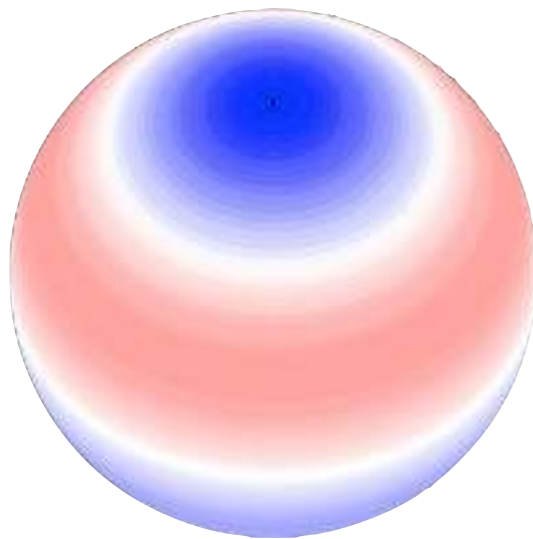
Asteroseismology 301

$(l,m)=(3,0)$
axisymmetric

$(l,m) = (3,2)$
tesseral

$(l,m)=(3,3)$
sectoral

Blue: Moving towards Observer Red: Moving away from Observer



Asteroseismology

time \longrightarrow frequency (period of mode)
geometry \longrightarrow spherical harmonic+radial order

$$\xi(r, \theta, \phi, t) = [(\xi_{r,nl} e_r + \xi_{h,nl} \nabla_h) Y_l^m(\theta, \phi)] \exp(-i\omega t)$$

Inferences of properties of stellar interiors via modes

a) requires frequencies & identification of (l,m) of as many modes as possible from data (+ n from models)

b) can only probe regions where modes propagate

Wave Equation

$$\frac{d^2 \xi_r}{dr^2} = \frac{\omega^2}{c^2} \left(1 - \frac{N^2}{\omega^2} \right) \left(\frac{S_l^2}{\omega^2} - 1 \right) \xi_r$$

$S_l =$ Lamb Frequency

$N =$ Brunt Vaisala Frequency

$c =$ Sound Speed

$\omega =$ Wave Frequency

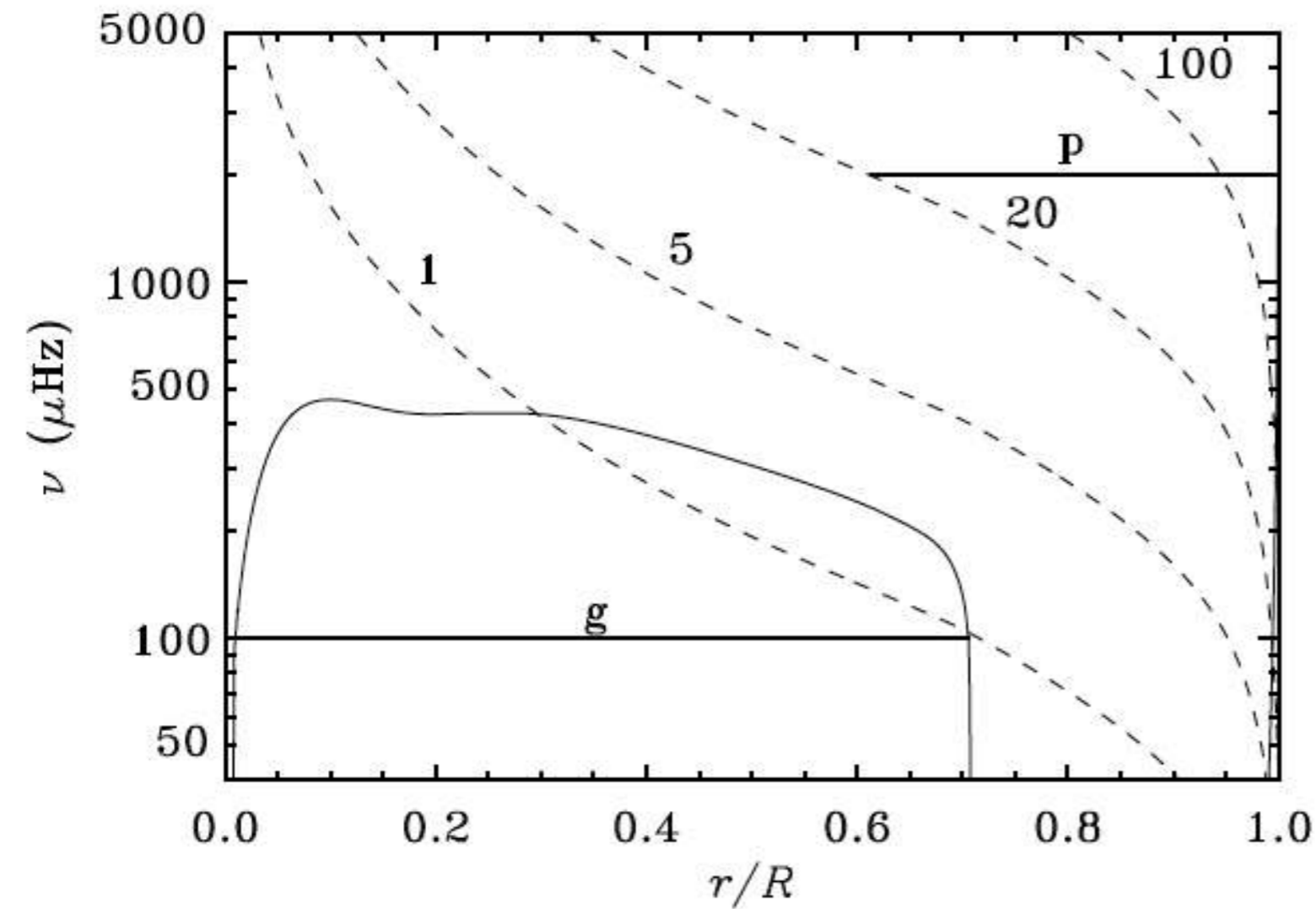
$|\omega| > |N|$ and $|\omega| > |S_l|$ **p-modes**

or

$|\omega| < |N|$ and $|\omega| < |S_l|$ **g-modes**

Otherwise waves are evanescent

Propagation Cavity in the Sun

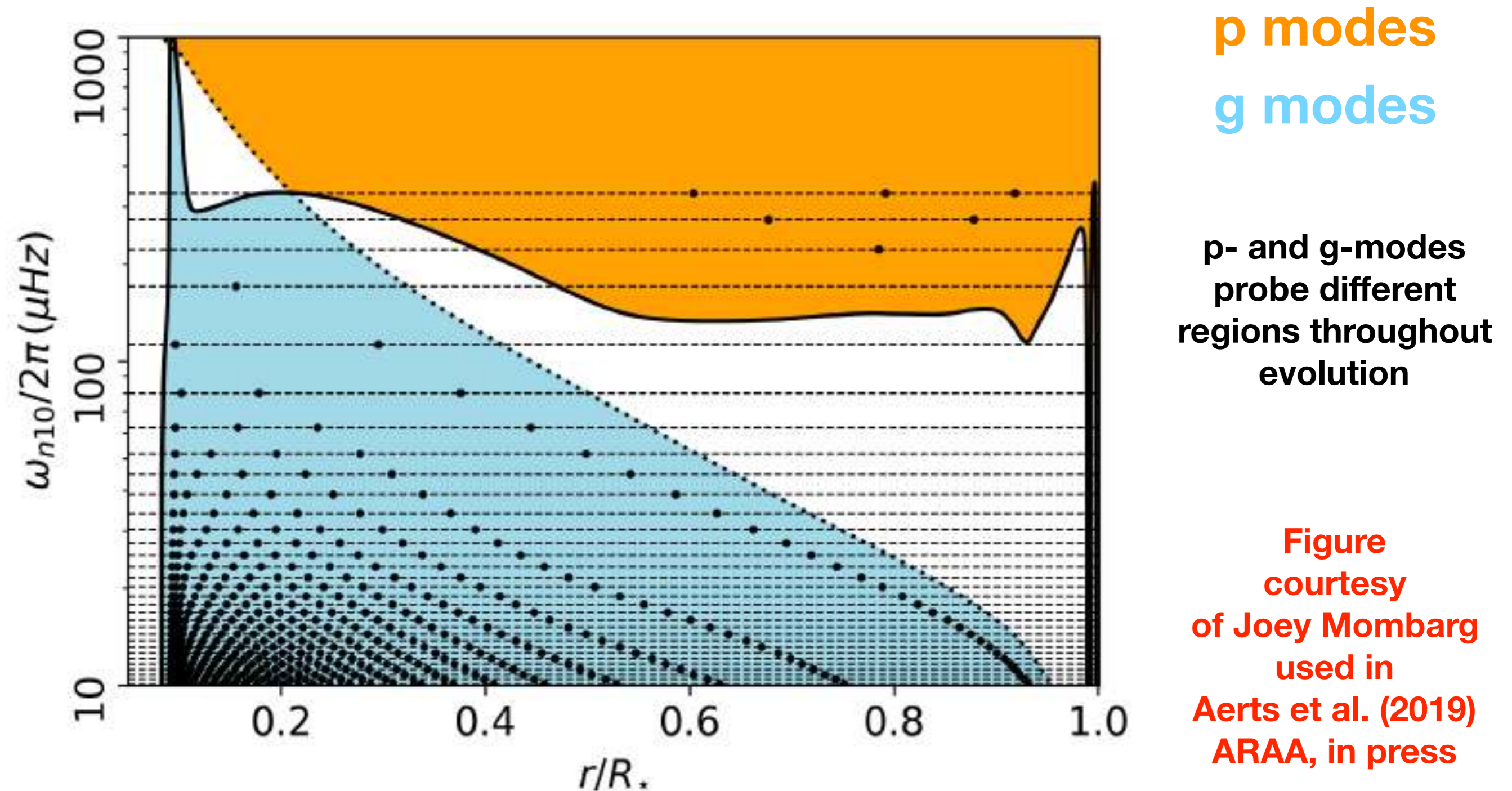


$$S_l^2 = \frac{l(l+1)c^2}{r^2}$$

$$N^2 \simeq \frac{g^2 \rho}{p} (\nabla_{\text{ad}} - \nabla + \nabla_{\mu})$$

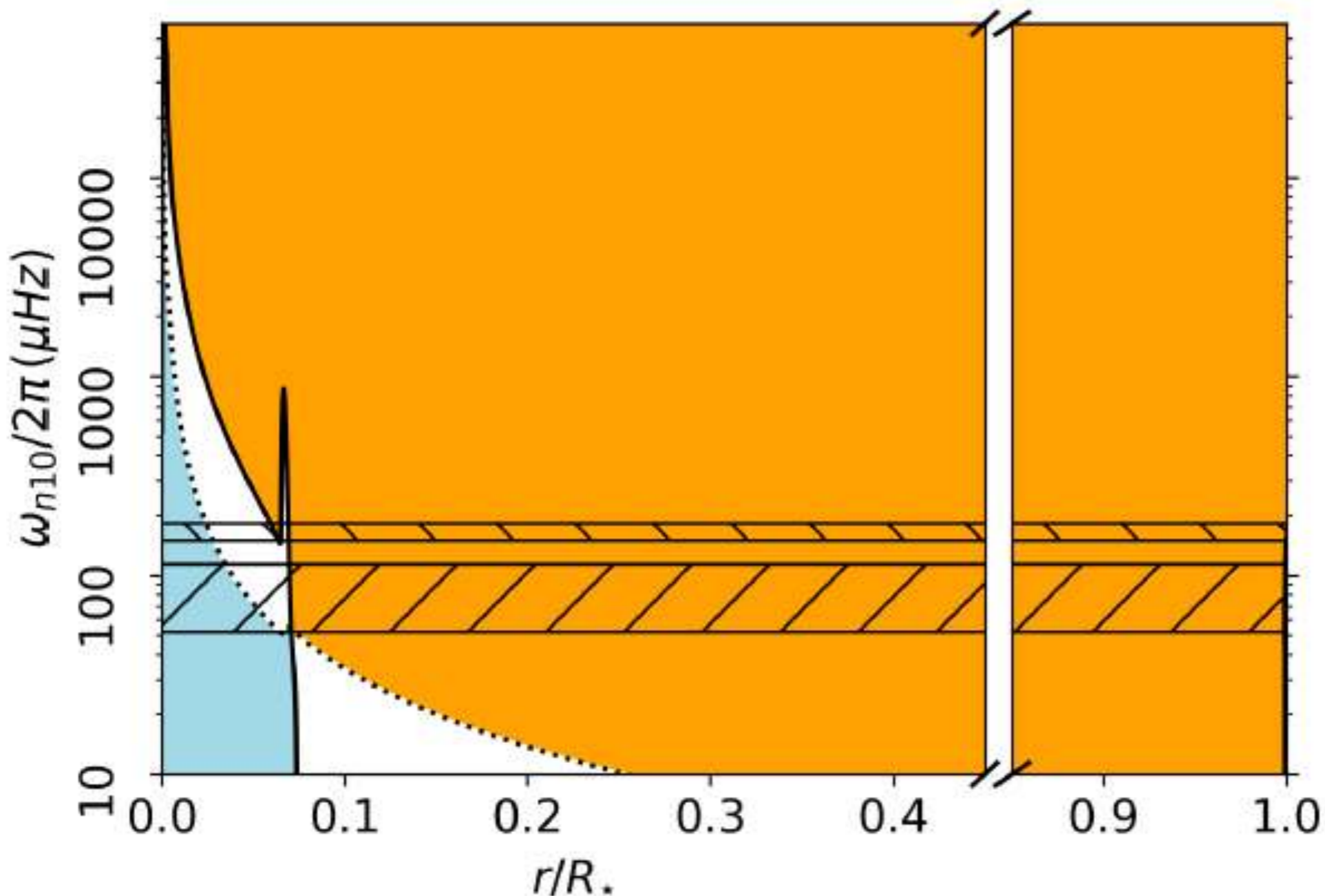
**All helioseismology is done with
p-modes**

Probing power in F stars (H burning in core)



Probing power on Red Giant Branch (H exhausted in core, burning in shell)

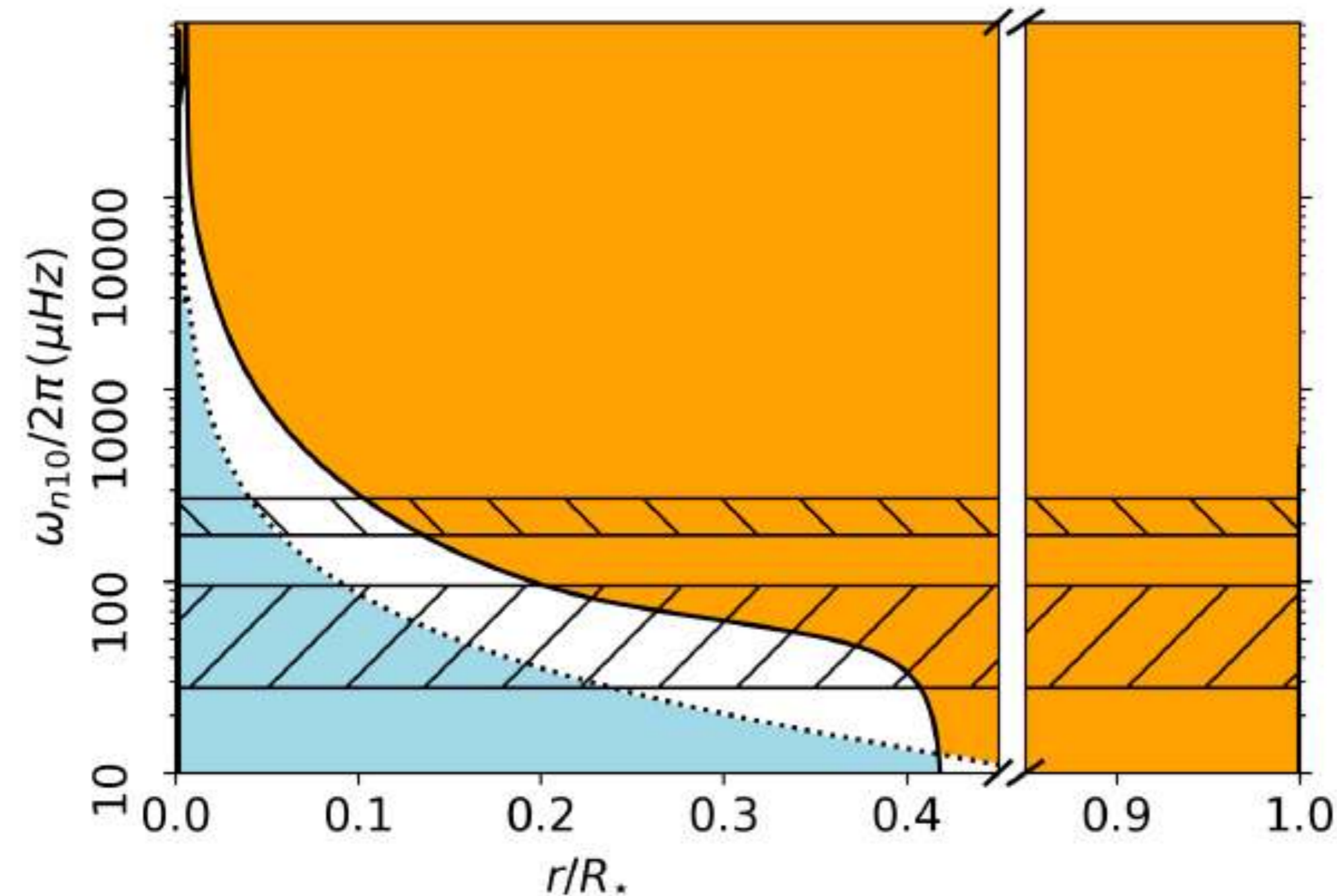
Main Sequence (H burning in core)



**p- and g-modes
probe different
regions throughout
evolution**

**Figure
courtesy
of Cole Johnston
used in
Aerts et al. (2019)
ARAA, in press**

Probing power on Red Clump (He burning in core)



**p- and g-modes
probe different
regions throughout
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**Figure
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Probing power of p- and g-modes

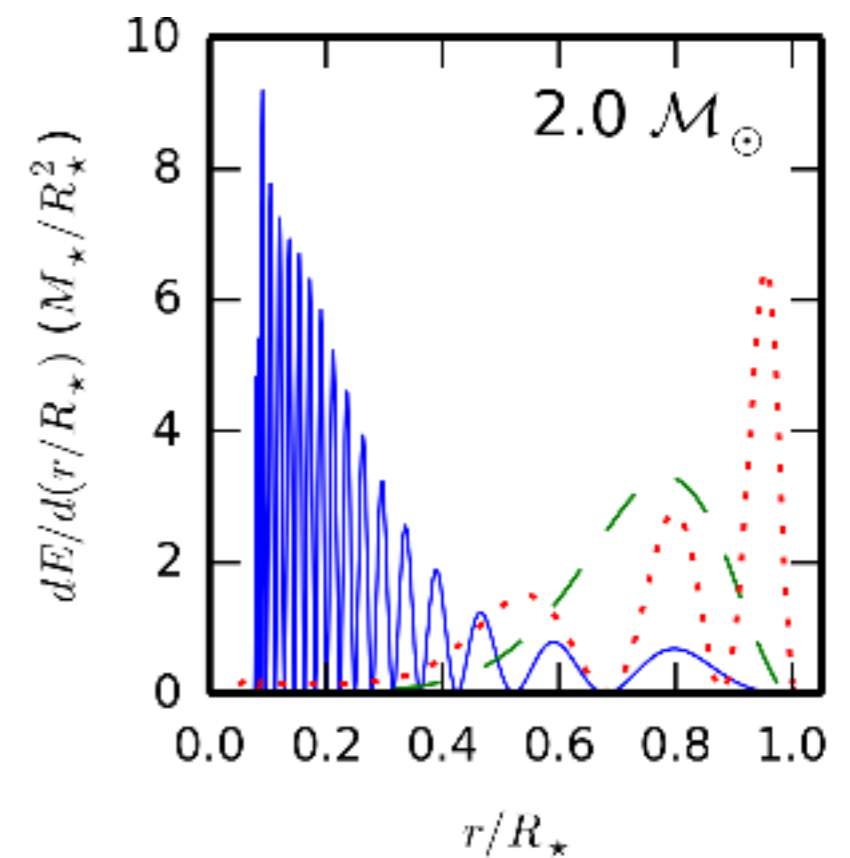
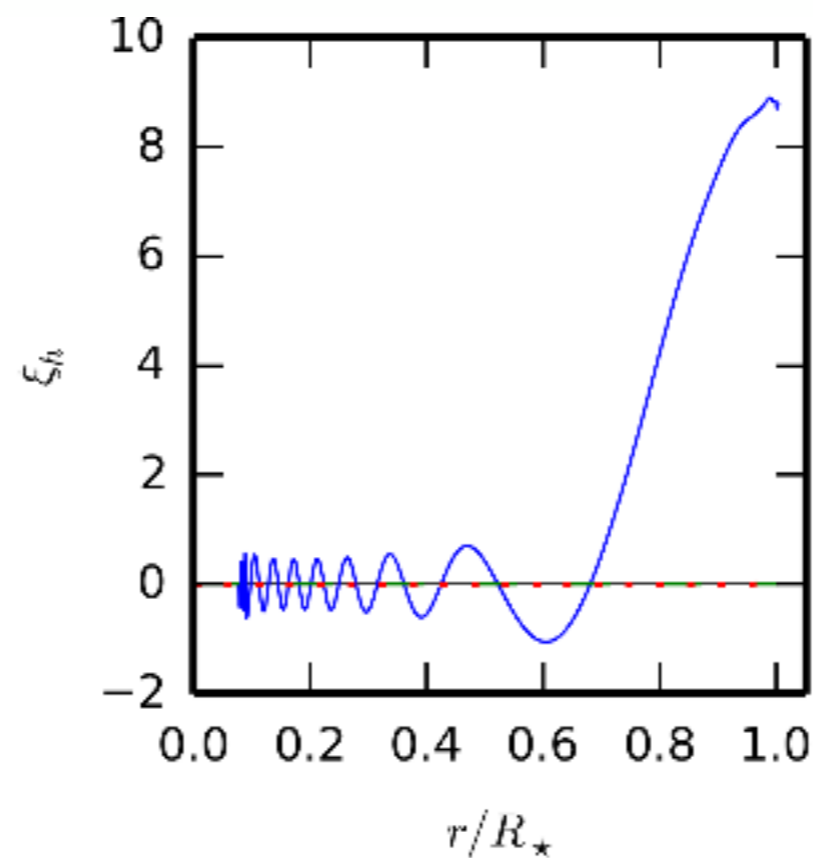
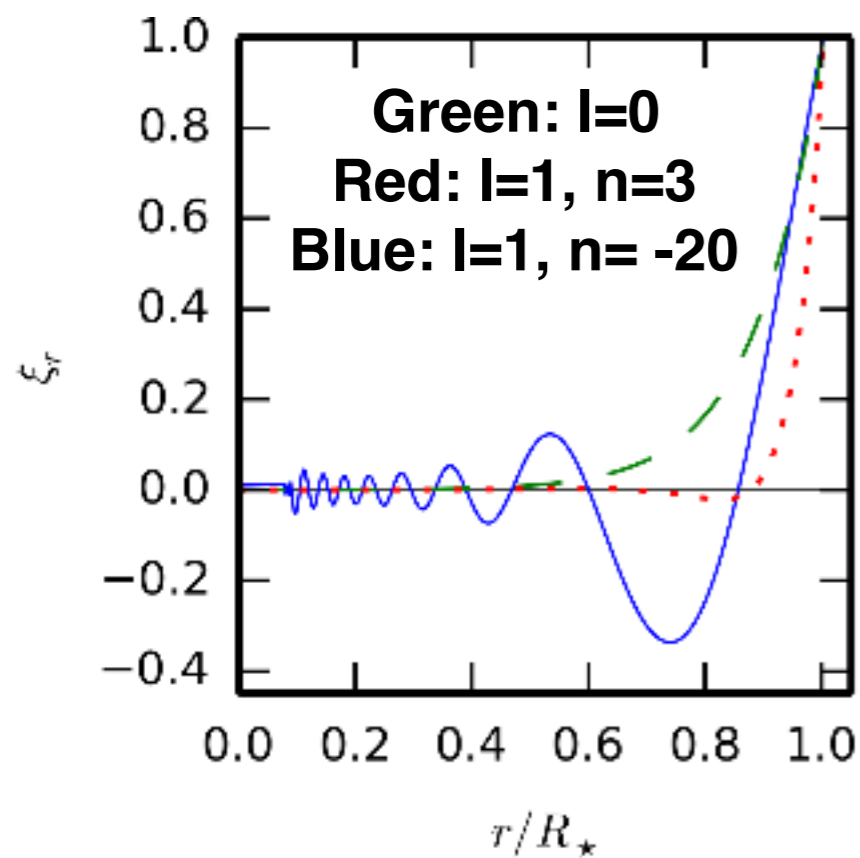


p-modes: dominantly radial ξ

g-modes: dominantly tangential ξ

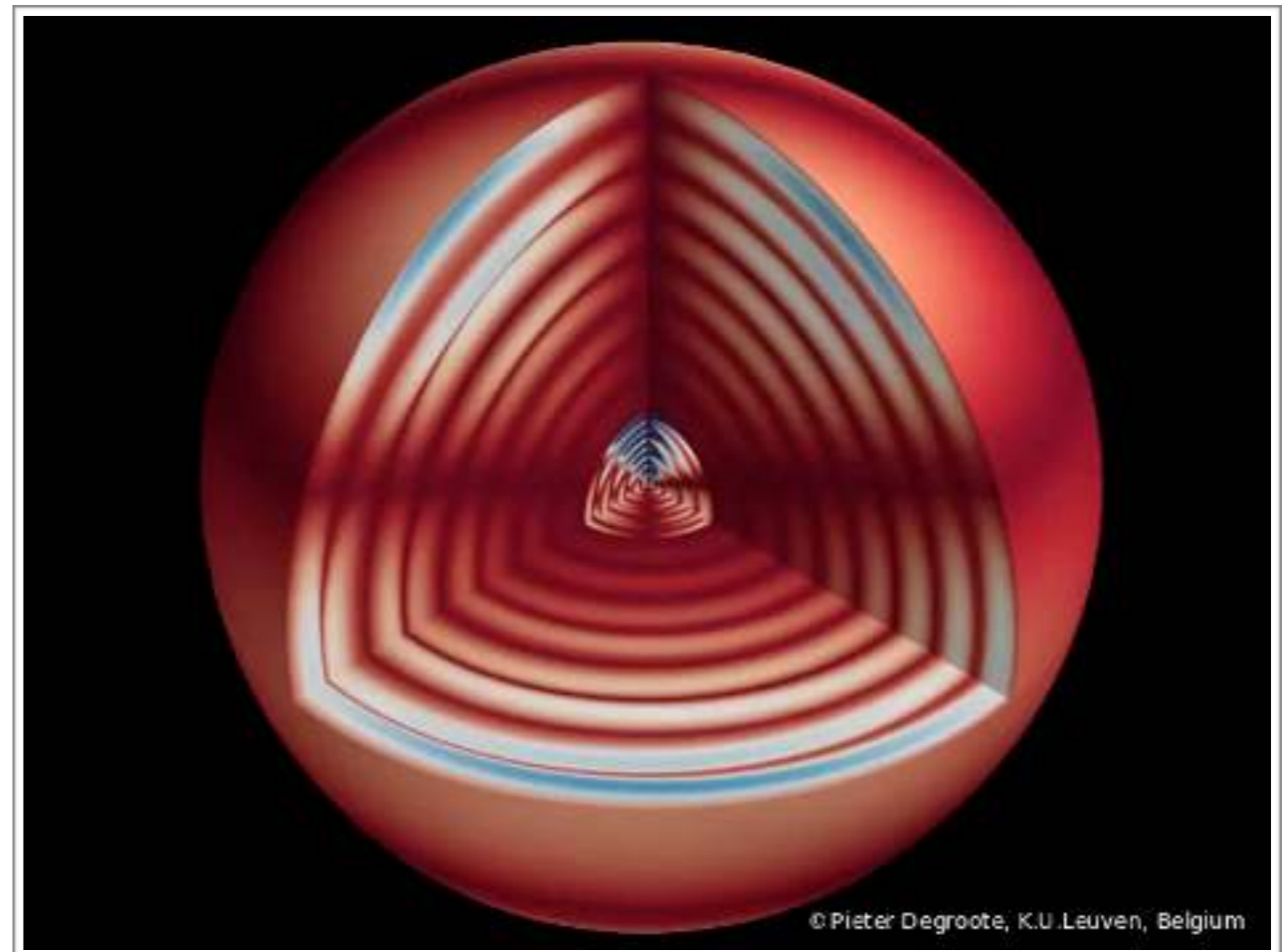
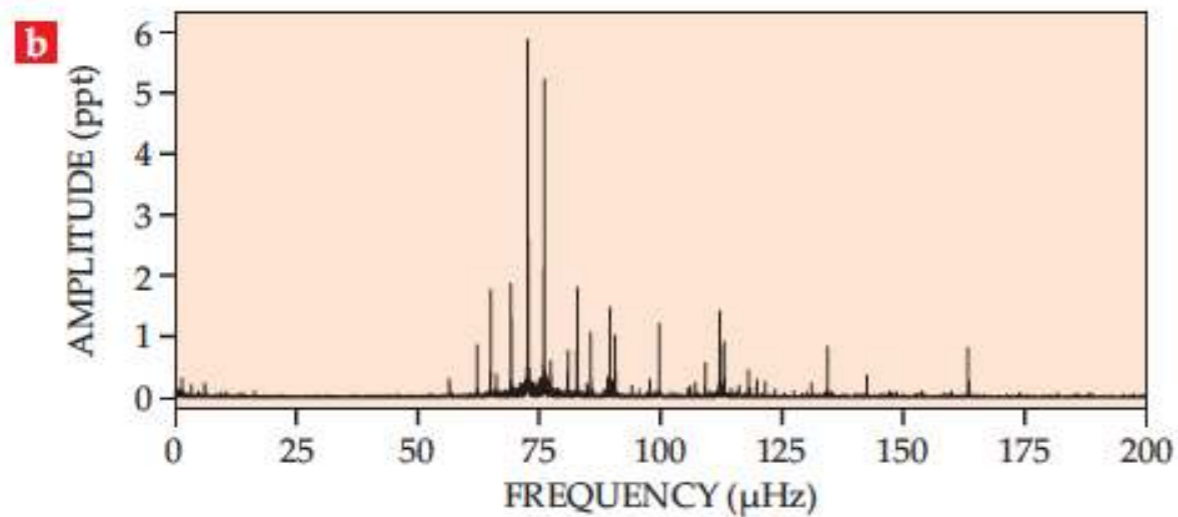
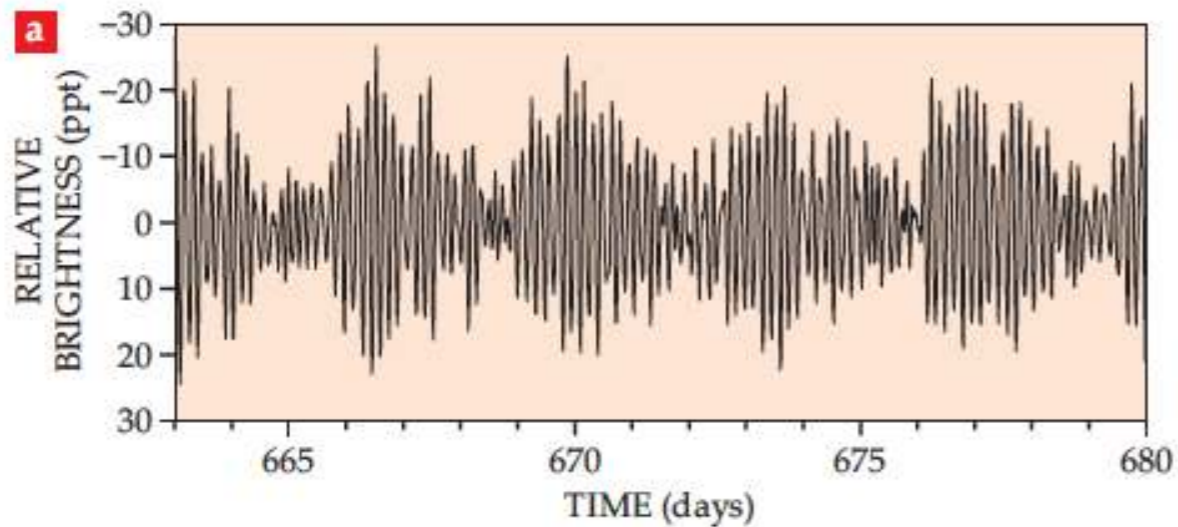
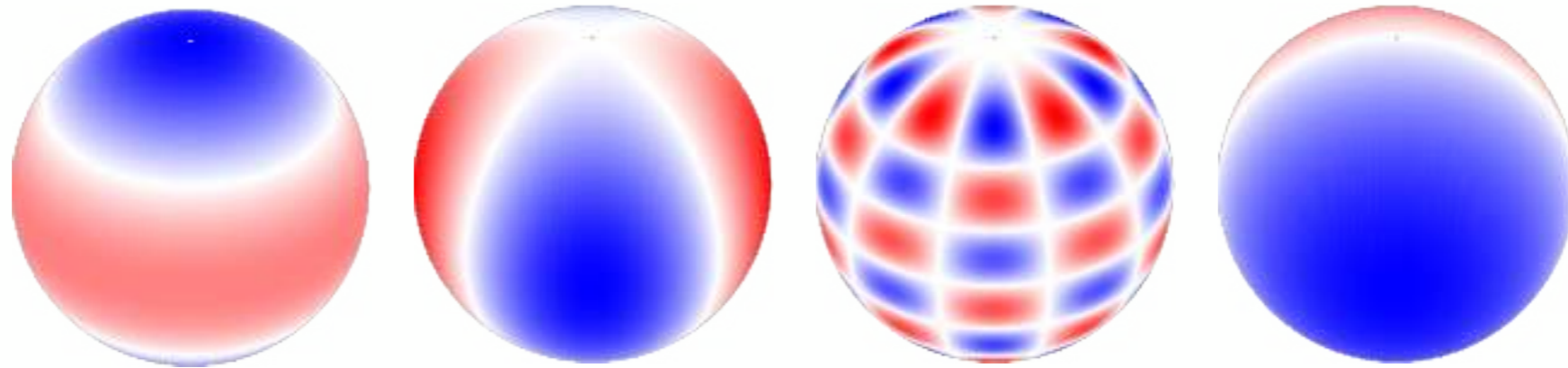
p-modes: probe envelope physics

g-modes: probe near-core region

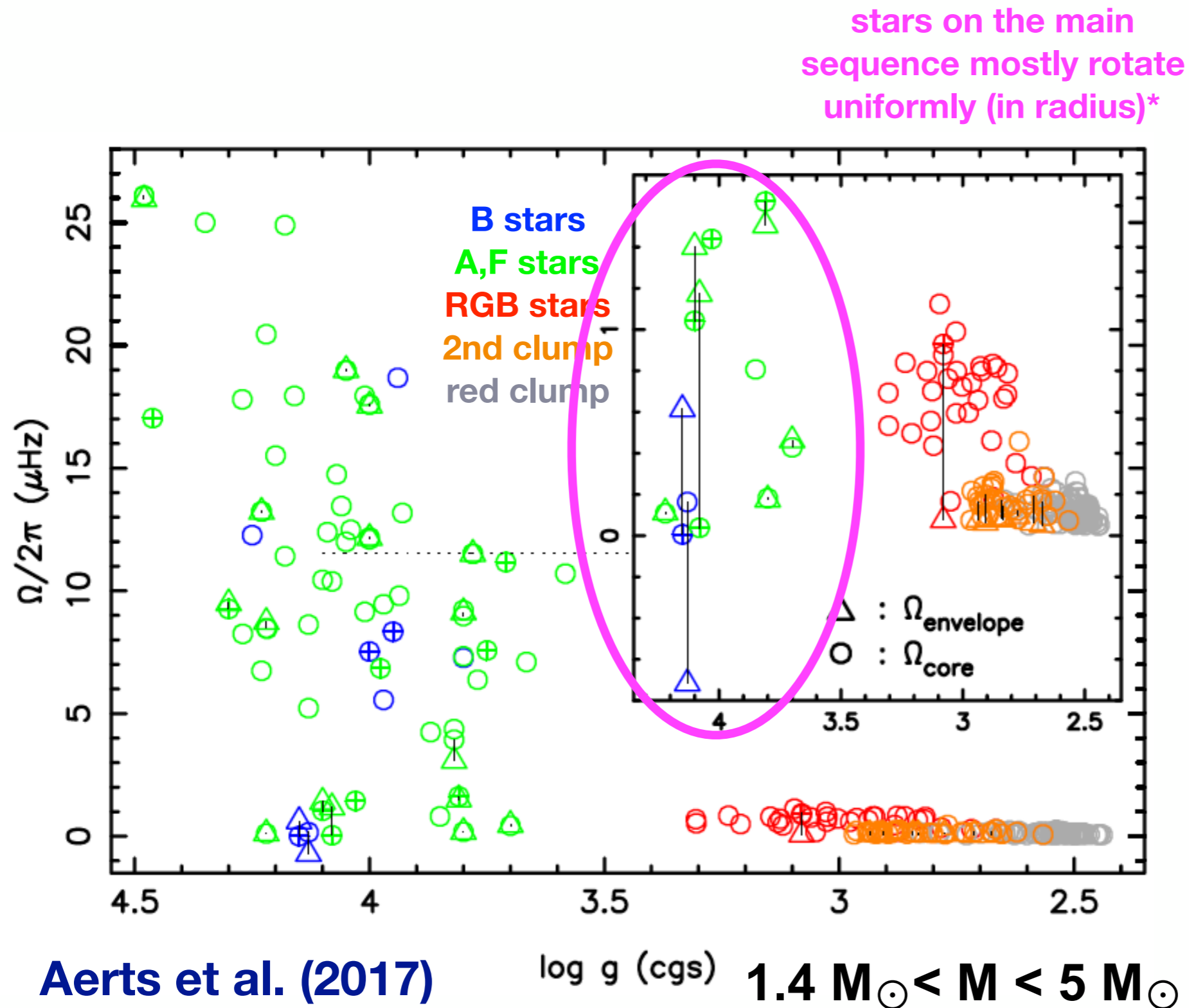


Schmid & Aerts (2016)

Starquakes and Asteroseismology



Rotation (and differential rotation) across the HR diagram

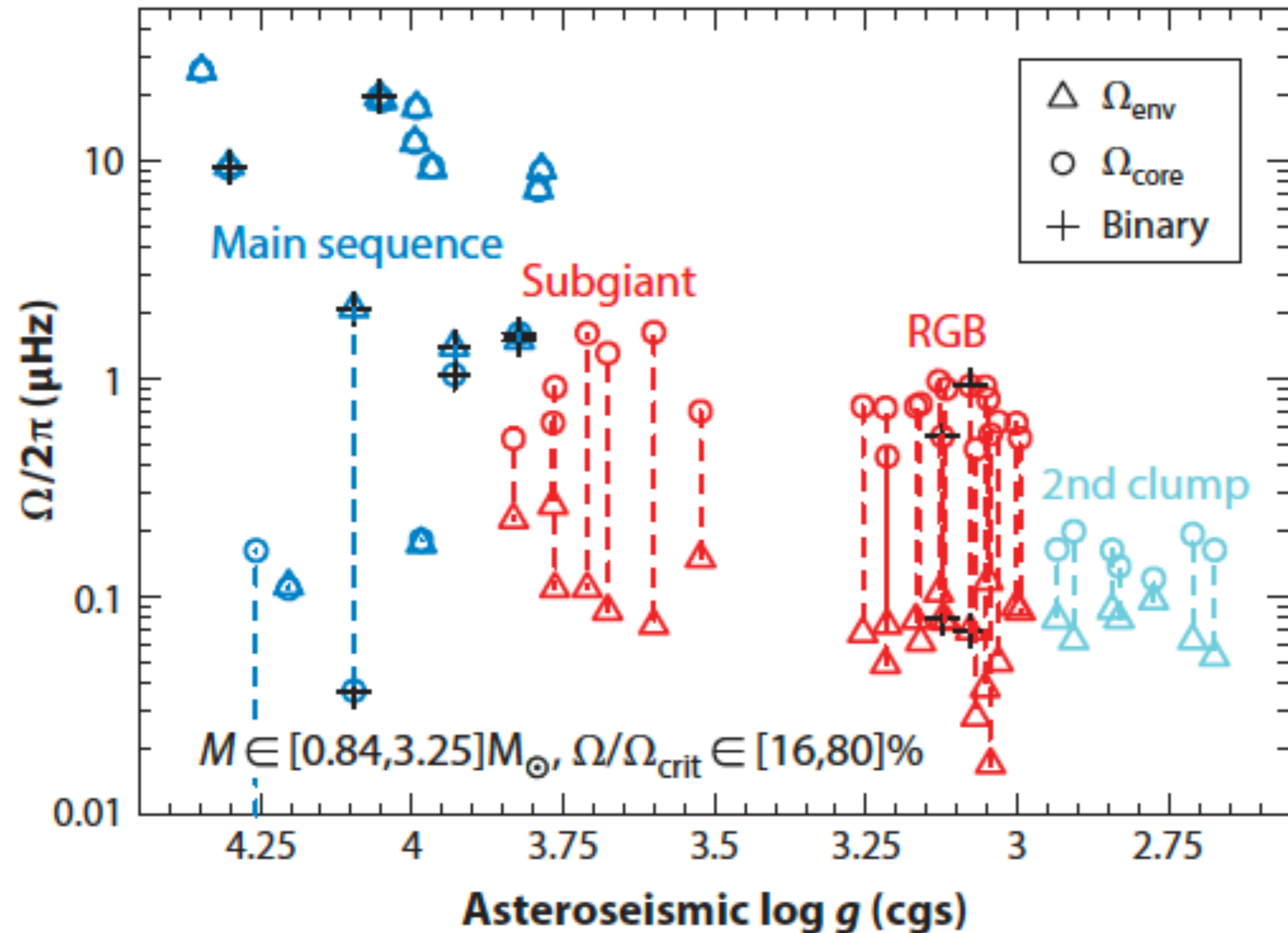


$\log g$ is a proxy for age

As stars age their cores spin up... but much less than expected

Must transfer angular momentum

Evolution of stellar rotation



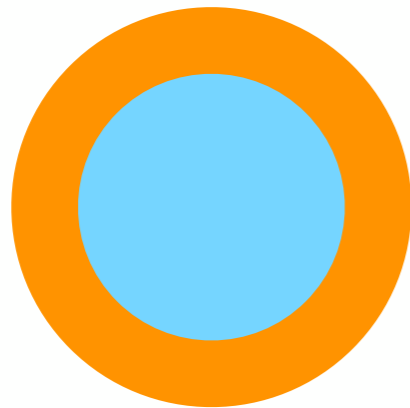
**Core rotation
much slower than
expected (by
10-100)
&
Differential
rotation
decreases**

Aerts et al. (2019), ARAA, Vol. 57, in press

RiA via <https://www.annualreviews.org/doi/pdf/10.1146/annurev-astro-091918-104359>

Post Main Sequence Evolution

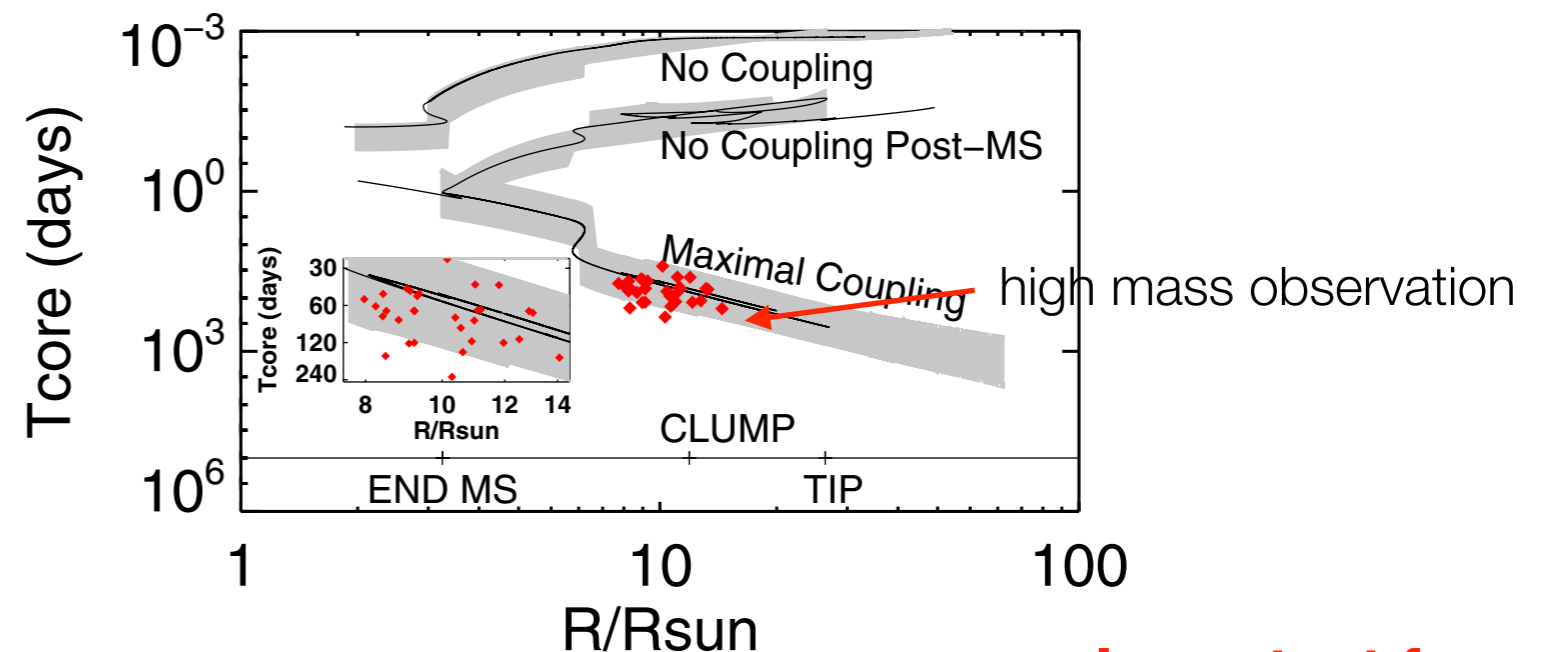
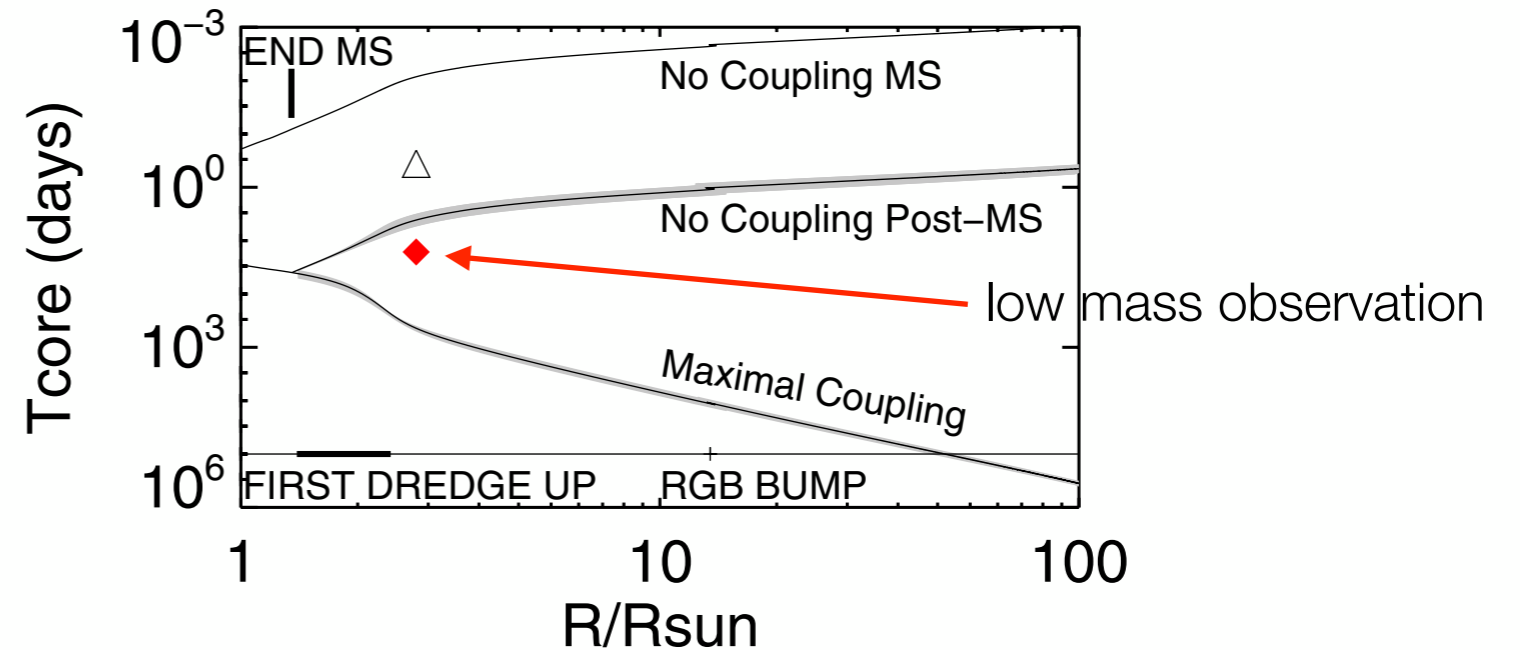
(happens for both low and high mass stars)



Energy source runs out in core;
lose pressure support; core
collapses

H starts burning in shell, causes
outer layers to expand

To conserve AM core would spin up
envelope would spin down
if no coupling



Tayar & Pinsonneault 2013

**Important from
IGW perspective**

Summary of Observations

- Observations of surface abundances indicates unknown mixing in a variety of stars (low and high mass)
- Helioseismology indicates coupling between convective and radiative regions in Sun and an efficient AM transporter in radiative region to cause uniform rotation
- Asteroseismology indicates efficient AM transporter between convective and radiative regions across all ages and masses, though possibly more efficient in intermediate/high mass stars
- All of this indicates we need better descriptions of (magneto-)hydrodynamic processes in stellar interiors

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Macroturbulence

On the origin of macroturbulence in hot stars

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INTERNAL GRAVITY WAVES IN MASSIVE STARS: ANGULAR MOMENTUM TRANSPORT

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